## Ring of Rings

## 12 Doubly-Linked Hexasons




Rins of Rinss: Twelve Doubly-Linked Hexasons

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Crease line - mark left by a crease that has been unfolded.

Folded or raw edge.

Paper seen from the edge.

Valley fold. Fold the paper toward you along this line.
-.-.-.-._. Mountain fold. Fold the paper away from you along this line.

X-ray line. A fold on an inner layer or layers of paper but not on the top layer. Also a hidden edge.


Fold arrow. Part of the paper moves in this direction to complete the fold.

Fold and unfold arrow. Make this crease, but return the paper to the way it was before the crease.


Unfold arrow. Part of the paper moves in this direction to undo one or more folds.


Fold and tuck into the pocket.

4 Push here.
$\triangleleft$ Open here.

Inflate here. Do this gently with fingers if the opening is large enough. Otherwise blow into the model. Do not spit. A long, thin, blunt tool may help.


Turn the model over from side to side.

Turn the model over from top to bottom.

Rotate the model. The arrows indicate the direction. An optional angle measurement indicates how far to rotate. If there's no angle indicated, just look at the next diagram!

New view from this side of the model.

The diagrams get larger. Your paper does not. The precise enlargement factor is optional.

The diagrams get smaller. Your paper does not. The precise enlargement factor is optional.

Landmark for this fold. The small mark allows the intersection, corner, edge, etc. to show through. These show up in pairs - fold here to there.

Detail work which is shown magnified.

Repeat this fold on another layer behind this one. The number of lines across the arrow indicate the number of repetitions.,


The units for the various hexagons are all closely related, taking advantage of a blintz corner that is non-structural and can be folded in numerous, decorative ways producing different color arrangements and different shapes and sizes for the gap in the center - or even affect the outer shape a bit. The variations shown are all diagrammed independently, so you can start with any of them. You will find their steps and assembly very similar; the first eight steps are the same. Step 9 starts work on that important blintz corner. The other blintz corner created with the roof fold in the second step could be folded to the back as a mountain fold for a bit more color variation and could even get a little more complicated but is much more limited than the one on the right hand side. Explore further variations on your own; there remains much to discover.


Changing the central hole makes more interesting hexagons, which generally cannot link doubly the way the Hexagonal Ring can. It is a tight fit with the largest central gap sported by the Hexagonal Ring. Other linkages are also possible and some variations with gaps only slightly smaller may link singly (passing through just the one ring to either side rather than the nearest two on each side).


All the versions have the same paper recommendation. They all work better with thicker paper such as memo cube, copy paper, scrapbooking paper or junk mail. This holds true even for small modules: 1" copy paper works fine, though it may be a bit smaller than most folders care to use. The paper recommendation is only that -- a recommendation for trying an unfamiliar model.

The Ring of Rings with seventy-two units provides a plethora of ways to arrange colors into patterns and even pictures. Recipes for some are provided. Explore more on you own, if you dare. Colorable blanks are provided after the recipes to help you test your own designs.

The fun doesn't stop there, Hexagonal Rings of different sizes can also link up or even nest. Fortunately, these projects require fewer units than the Ring of Rings, coming in at 24, 42 and $6 n$ (where $n$ is the number of nested hexagons).



RAT mountain fold to hide corner.
9.


Bisect the angle. (Fold only the top layer.)


Fold square corner to obtuse (blunt) corner.



Bisect the angle. TRADE OFF: This valley fold trades a folded edge on the front to remove an odd little bit of color change on the back.
11.


Unfold one crease.


Mountain fold the existing crease to complete the unit.
13.


Result. Fold six (6) of these.


Slide the units into each other, interleaving the layers of paper.
The brown flap with the colorful square corner which is sandwiched between layers of its own flap goes into the pocket of the orange unit. The back flap of the orange unit goes behind the brown unit. It doesn't quite fit right if you put it put it in front of the yellow square corner showing on the brown unit.



Recommended Paper: Six (6) thick $1.5-3 "(40-75 \mathrm{~mm})$ squares.

The unit for this wreath has a blintz corner that is non-structural and can be folded in many different ways to create variations on this model.

3.


Fold only the top layer.


Fold corner to corner and unfold.
5.


Bisect the angle.


RAT mountain fold to hide corner.


Fold square corner to obtuse (blunt) corner.


Bisect the angle. (Fold only the top layer.)


Unfold one crease.


Mountain fold the existing crease to complete the unit.


The Triple Hex unit.
Fold 6 and assemble like Starry Space.



Slide the units into each other, interleaving the layers of paper.
The teal flap with the colorful square corner which is sandwiched between layers of its own flap goes into the pocket of the brown unit. The back flap of the brown unit goes behind the teal unit. It doesn't quite fit right if you put it put it in front of the yellow square corner showing on the teal unit.

 2.


Fold only the top layer.

The unit for this wreath has a blintz corner that is non-structural and can be folded in many different ways to create variations on this model.


Fold corner to corner and unfold.

Recommended Paper: Six (6) thick $1.5-3 "(40-75 \mathrm{~mm})$ squares.
3.

5.


Bisect the angle.


RAT mountain fold to hide corner.


Fold square corner to obtuse (blunt) corner.



Bisect the angle. (Fold only the top layer and unfold.)

10.


Bisect the new angle.
(Fold only the top layer.)

Mountain fold the existing crease to complete the unit.


The $4^{\text {th }}$ variant. Fold six (6) to assemble.



Slide the units into each other, interleaving the layers of paper. The teal flap with the colorful square corner which is sandwiched between layers of its own flap goes into the pocket of the green unit. The back flap of the green unit goes behind the teal unit. It doesn't quite fit right if you put it put it in front of the yellow square corner showing on the teal unit.
17.



The unit for this wreath has a blintz corner that is non-structural and can be folded in many different ways to create variations on this model. Those that do not change the shape of the ring can be used for the Ring of Rings; others are decorative as single rings, as is the case with Starry Space.

Recommended Paper: Six (6) thick $1.5-3 "(40-75 \mathrm{~mm})$ squares.
3.


2.


Fold only the top layer.


Fold corner to corner and unfold.
5.


Bisect the angle.


RAT mountain fold to hide corner.


Fold square corner to obtuse (blunt) corner.


Bisect the angle.


Refold



The new violet unit overlaps the other violet unit and should land on top of it. Add the other three (3) units in the same manner. If you are making a single ring, also close the ring in the same way. For a Ring of Rings, leave each individual ring open to link it with other rings, but it likes to spring into a snake and fall apart, so push the top end behind the other end so tension holds it temporarily.

Slide the units into each other, interleaving the layers of paper.
The mauve flap with the colorful square corner which is sandwiched between layers of its own flap goes into the pocket of the violet unit. The back flap of the violet unit goes behind the mauve unit. It doesn't quite fit right if you put it put it in front of the yellow square corner showing on the mauve unit.


To make a lone ring, close the ring in the same way. For a Ring of Rings or other linked structure, leave each individual ring open for now, but tuck the top end behind the other end for a temporary hold.


The units for the Hexagonal Ring, Starry Space, Hex Vortex, Triple Hex and practically any other of the myriad minor variants are interchangeable because they all attach the same way. Mix up different variants at your own risk. Try to turn the center into a triangle instead of a hexagon or star using two variants!



A subset of variations on the Hexagonal Unit can also form the Ring of Rings. More importantly, they can be incorporated among the standard units as specialty units to add detail to representational drawings. Many of these specialty units utilize the kasane technique.

There is one notable specialty unit that cannot form a Ring of Rings. The Pointy Specialty Unit to add hair, cat ears or horns changes the outer shape of the hexagon. The Ring of Rings accommodates it only on the outer rim. Elsewhere the points would get thoroughly bashed trying to go through other rings and munged out of the way rather than neatly folded out of the way. Even on the outer rim, the method of adding the no-longer-perfectly-hexagonal ring requires a bit of modification to avoid bashing the corner.


All the variations of the hexagonal unit love thick paper. Even $1 "$ ( 25 cm ) squares prefer 20281b. copy paper to kami. Most of the examples for Ring of Rings Recipes used such 1" paper. This implies wiggle room for at least a couple layers of thinner paper. Laminating thinner papers into a thicker paper would work well and allow much greater control of duo colors and textures. That gluing and cutting operation is more (and messier) work than necessary.

Kasane (pronounced kah-sah-nay) folding - folding multiple layers of paper - is a simpler and more flexible option. The edges of the basic Hexagonal Units (for the Hexagonal Ring that makes the Ring of Rings, Ringed Planet, Chaos Theory and Nestagons) hide well, so when paper creep would show the layer beneath, the effect mostly hides. Some of the other variations might be able to use this effect decoratively with thin duo papers.

Simple kasane units just treat the two (or more) layers as one. Unlike laminated paper, these layers can fold separately, allowing divergent folds to further control the color change scheme for even more creative patterns. Representational drawings can use this for greater resolution and little shapes that would otherwise be unavailable, such as the winking eye.

For more information kasane folding, see Eric Kenneway's classic "Complete Origami A-Z."

This is a specialty variation of the Hexagonal Unit primarily for use on the rim of the Ring of Rings; but which can of course also form a stand-along six-unit wreath. The point changes the shape enough that this unit cannot substitute for the Hexagonal Unit everywhere in the Rings. Take care not to bash the corner when linking.

This specialty unit adds hair, cat ears and horns to various emoji.

2.


Fold only the top layer.


Fold corner to corner and unfold.


Bisect the angle.


RAT mountain fold to hide corner.


Fold square corner to obtuse (blunt) corner.



For your first Ring of Rings, it is easiest to make twelve (12) single color Hexagonal Rings of various colors. You can better see which ring is passing through which other rings this way. More interesting color patterns abound. Recipes for some follow the Ring of Ring instructions..


Options:
one (1) ring of each of twelve (12) colors two (2) rings of each of six (6) colors three (3) rings of each of four (4) colors

You will need half a gross (72) of units. 2.5 "-3.5" memo cube, copy paper or even scrapbooking paper are great ways to start. Even small, this model loves thick paper!


Close the first ring.



Start with the one closed ring (left). Unhook the temporary hold on the next ring counting clockwise around the Ring of Rings. Take the end with sandwiched tab (marked with a smiley face) and thread it through the closed ring from the top. Close the ring.

 through tenth $\left(10^{\text {th }}\right)$ units link more easily.

As more units accrue, it becomes noticeably easier to pass exactly two (2) units of the end marked with the smiley face through the preceding rings. For the final rings, it is vital. For these solid color rings, it only affects the ease of assembly, but for more complex patterns, it is essential for keeping track of the proper rotation of each hexagonal ring.




Depending on the size, thickness and slickness of your paper, the Ring of Rings will have more or less play in it. Adjust it to nice symmetry from both front and back (see next diagram). If it has too much play in it (feels too loose, constantly needs readjusting), use thicker paper next time. Even with very small units (e.g. 1" paper), thicker paper (such as copy paper) is preferable to kami.


## Done!



Solid color rings of one- or two-tone paper provide quite rewarding results, but those rings lock tightly enough in place, so there is no reason to restrict rings to only one paper each. Complexity beacons. Far more intricate designs are possible with multiple colors. These patterns and drawings require precise control of the rotation of each ring in the Ring of Rings. The first few rings flop about and must be controlled very consciously so they stiffen into the right places as more rings join them, but latter rings become automatic by leaving the temporary opening of each ring such that just two units should pass through the preceding two rings.

Knowing what to put where can also get finicky. Changing the plan on the fly is difficult because of the two stages of assembly. Practice helps, but so can the following recipes and planning tools in the form of coloring pages.

The recipe list is in order of approximate difficulty starting with the easiest patterns. Cut the paper as shown, substituting colors as you please. Fold units for the Hexagonal Rings from that paper and assemble into the rings shown with the gap where shown. Assemble the Ring of Rings; if there is more than one color pattern of hexagon, follow the specific order shown,




ToS




ToS




TOS





There's a hole,
there's a hole,
there's a hole in the
square peg in the
round hole...


ToS





Be careful of units that are the inverse of other units.


ToS






Jos






B


## ToS









Here's a blank Ring of Rings to print and color to figure out your own color patterns. Try to keep the constraints of the paper in mind. Afterward, the surrounding square makes it easy to turn your plan into a square for origami with the pattern centered.


For some patterns, the reverse side becomes the favored front, so here's the back to color and work out new patterns. Cut out on the square to fold your worksheet afterward.


Here are individual rings to color to make notes for your new designs in the preceding Ring of
FOS Rings. The larger rings are the same size as the ones in the Ring of Rings. Fold these expended notes afterward - use either squares or hexagons! Use the smaller rings for expedited note-taking.


held


Bring the marked end of the red hexagon up through the center of the green hexagon and close the red hexagon around the upper left side of the green hexagon.


Bring the marked end of the orange hexagon down through the center of the red hexagon and close it.


From behind the green hexagon, bring one unit of the marked end of the yellow hexagon down through the center of the orange hexagon and then up through and over the side of the green unit and close it. The links will retain only a little amount of play.


For planning purposes and folding afterward...


Bring the marked end of the red hexagon down through the center of the white hexagon and close the red hexagon.


Bring the marked end of the orange hexagon up through the white hexagon and down through the red hexagon. Close the orange hexagon.


Bring the marked end of the yellow hexagon down through the white hexagon and orange hexagon simultaneously. Close the yellow hexagon.


Bring the marked end of the blue hexagon down through the white hexagon and green hexagon simultaneously. Close the blue hexagon.


Bring the marked end of the green hexagon up through the white hexagon and down through the yellow hexagon. Close the green hexagon.


Bring the marked end of the purple hexagon up through the white hexagon and down through the blue hexagon. Bring the other end of the purple hexagon up through the red hexagon. It may be easier to remove one unit and replace it once the end is threaded through the red hexagon. Close the purple hexagon. Check all the joints and tighten any that have loosened and tweak the symmetry. The rings fit quite but not absolutely tightly.


For planning purposes and folding afterward...

$w_{0}$

$w_{1}=1.5 w_{0}$

| $w_{0}$ | $1 "$ | 32 mm |
| :---: | :---: | :---: |
| $w_{1}$ | $1 / 1 / 2 "$ | 48 mm |
| $w_{2}$ | $2^{1 / 1 / 4}$ | 72 mm |
| $w_{3}$ | $3^{3 / 8} 8^{\prime \prime}$ | 108 mm |
| $w_{4}$ | $5^{1 / 16 "}$ | 162 mm |
| $w_{5}$ | $7 \frac{19}{3} 32^{\prime \prime}$ | 243 mm |

Example progressions


Use any variant for the smallest hexagon.


Attach the growing nest inside the next larger hexagon, tucking the corners into the pockets. Repeat for all hexagons to complete the nest.


Done... iff $n=4$.


Toऽ
Done... iff $n=5$.


Joc


Plan your nests, then fold your expended plans afterward. The squares are centered on the hexagons for convenient cutting.



Toऽ


$w_{1}=2 w_{0}$ or slightly less


Exactly doubling the size of the squares produces hexagons that are the size of the inner hexagons they go into. Rotated, they catch, but using $17 / 8$ as the multiplier and the rounding slightly for more convenient measuring makes the connection more solid and the slower growth becomes significant and helpful for deeper (higher order) nests.

Hex Vortex, Triple Hex and other possible variants with the nonstructural corner likewise flipped center-ward can next in exactly the same way.


Attach the smallest hexagon inside the next smallest, tucking the corners into the pockets.


Attach the growing nest inside the next larger hexagon, tucking the corners into the pockets. Repeat for all hexagons to complete the nest.


Done... iff $n=3$.



Done... iff $n=4$.



These two pages of blank Starry-Eyed Nestagons to help you figure out your own color patterns. Print, color, and afterward the surrounding square makes it easy to re-purpose your plan as a square of origami paper with the pattern centered. The hexagons suggest themselves as a paper shape, too


The Nestagon and the Starry-Eyed Nestagon can use any version of the hexagon at the center even though they use different inner edges to trap the next smaller hexagon. These inner edge hexagons differ in size if not usefulness and calculating the size of paper for the nest larger hexagon differs accordingly depending only on the type of the entrapping hexagon and and the size of the hexagon to grip but not on the type of any smaller hexagon. Therefore, it is possible to mix and match the types of hexagons at each level of a single nest. Just remember to calculate the size with the appropriate formula.

The Starry-Eyed Nestagon includes a comment that Hex Vortex and Triple Hex would build nests they same way as Starry Space. The essential difference goes back to the non-structural corner which is so very useful for decorative variation. The corner is either flipped toward the outer edge of the hexagon or towards its center. This is a binary decision so any hexagon ring that uses units that are all in one category or the other - innie or outie - will have one of these hexagonal pockets and can therefore be used at any level of a nest. These units are mix and match, so some hexagonal rings could use units of both types. Such mongrel rings can always be the center ring. If every second ring is an innie or an outie, the hexagon may still be able to grip a smaller hexagon by three non-adjacent corners.

So much to explore...


TOS
77


Toऽ


Slide the units into each other, interleaving the layers of paper with the top layer of the northern unit on top


Mountain fold with the existing crease from step 4.


Turn over and continue adding units counterclockwise. Temporarily opening step 14 will let you work clockwise instead.


Steps 9-12 provide decoration independent of structure. Many variations are possible. Here are a few to get you started.
Assemble them the same way as Starry Space. Mix or match in each hexagon.


Bisect the angle.


Unfold one crease.

The Triple Hex unit.
Fold 6 and assemble like Starry Space.


Bisect the angle.
Bisect the new angle.
Unfold one crease.

The $4^{\text {th }}$ variant. Now create your own!


Slide the units into each other, interleaving the layers of paper. The mauve flap with the colorful square corner which is sandwiched between layers of its own flap goes into the pocket of the violet unit. The back flap of the violet unit goes behind the mauve unit. It doesn't quite fit right if you put it put it in front of the yellow square corner showing on the mauve unit.


The new violet unit overlaps the other violet unit and should land on top of it. Add the other three (3) units in the same manner. If you are making a single ring, also close the ring in the same way. For a Ring of Rings, leave each individual ring open to link it with other rings, but it likes to spring into a snake and fall apart, so push the top end behind the other end so tension holds it temporarily.


To make a lone ring, close the ring in the same way. For a Ring of Rings, leave each individual ring open for now, but tuck the top end behind the other end for a temporary hold.

